## Lesson 1-9: Exponents

The base a is raised to the power of n is equal to the multiplication of $\mathrm{a}, \mathrm{n}$ times:

$$
\begin{array}{r}
a^{n}=a \times a \times \ldots \times a \\
n \text { times }
\end{array}
$$

a is the base and n is the exponent.

## Examples

$$
\begin{aligned}
& 3^{1}=3 \\
& 3^{2}=3 \times 3=9 \\
& 3^{3}=3 \times 3 \times 3=27 \\
& 3^{4}=3 \times 3 \times 3 \times 3=81 \\
& 3^{5}=3 \times 3 \times 3 \times 3 \times 3=243
\end{aligned}
$$

Exponents rules and properties

| Rule name | Rule | Example |
| :---: | :---: | :---: |
| Product rules | $a^{n} \cdot a^{m}=a^{n+m}$ | $2^{3} \cdot 2^{4}=2^{3+4}=128$ |
|  | $a^{n} \cdot b^{n}=(a \cdot b)^{n}$ | $3^{2} \cdot 4^{2}=(3 \cdot 4)^{2}=144$ |
| Quotient rules | $a^{n} / a^{m}=a^{n-m}$ | $2^{5} / 2^{3}=2^{5-3}=4$ |
|  | $a^{n} / b^{n}=(a / b)^{n}$ | $4^{3} / 2^{3}=(4 / 2)^{3}=8$ |
| Power rules | $\left(b^{n}\right)^{m}=b^{n \cdot m}$ | $\left(2^{3}\right)^{2}=2^{3 \cdot 2}=64$ |
|  | ${ }_{b} n^{m}=\mathrm{b}\left(n^{m}\right)$ | ${ }_{2} 3^{2}=2\left(3^{2}\right)=512$ |
|  | ${ }^{m} \sqrt{ }\left(b^{n}\right)=b^{n / m}$ | ${ }^{2} \sqrt{ }\left(2^{6}\right)=2^{6 / 2}=8$ |
|  | $b^{1 / n}=n b$ | $8^{1 / 3}=\sqrt{3}^{8}=2$ |
| Negative exponents | $b^{-n}=1 / b^{n}$ | $2^{-3}=1 / 2^{3}=0.125$ |
| Zero rules | $b^{0}=1$ | $5^{0}=1$ |
|  | $0^{n}=0$, for $n>0$ | $0^{5}=0$ |
| One rules | $b^{1}=b$ | $5^{1}=5$ |
|  | $1^{n}=1$ | $1^{5}=1$ |

